

Topological Relationship Identification in 3D Cadastre

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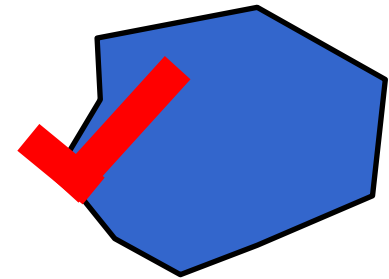
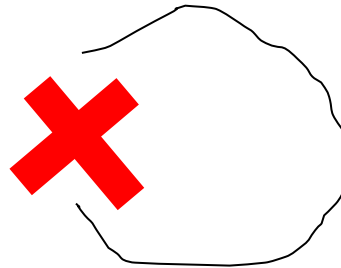
2012/10/26

1 INTRODUCTION

CADASTRE SPACE (the space of a parcel unit)

Connected

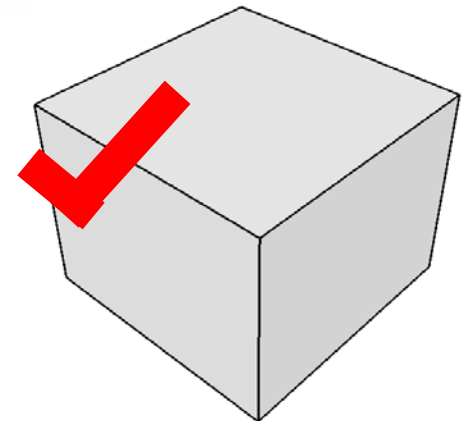
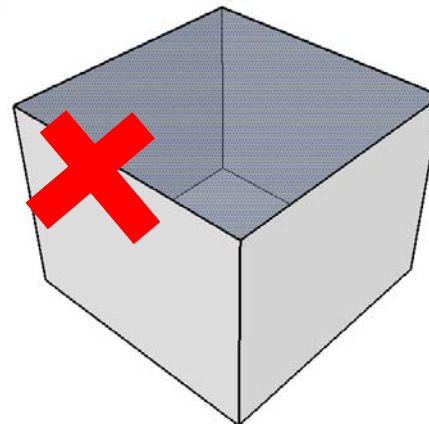
2D



Closed

homogenous

3D



1 INTRODUCTION

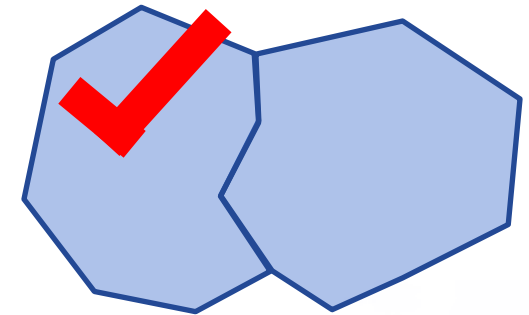
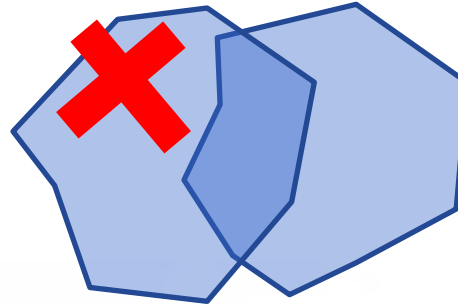
CADASTRE SPACE (the space among parcel units)

Unique

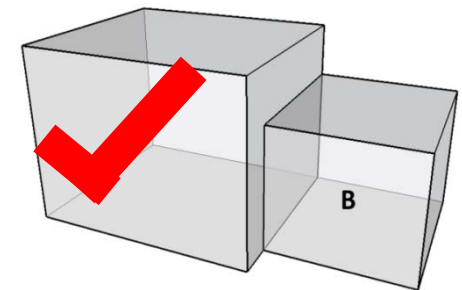
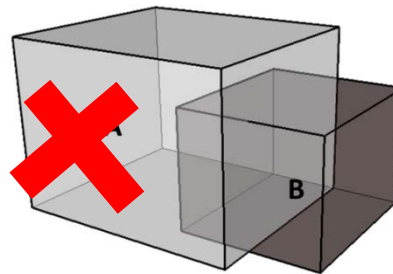
Exclusive

no overlap

2D



3D



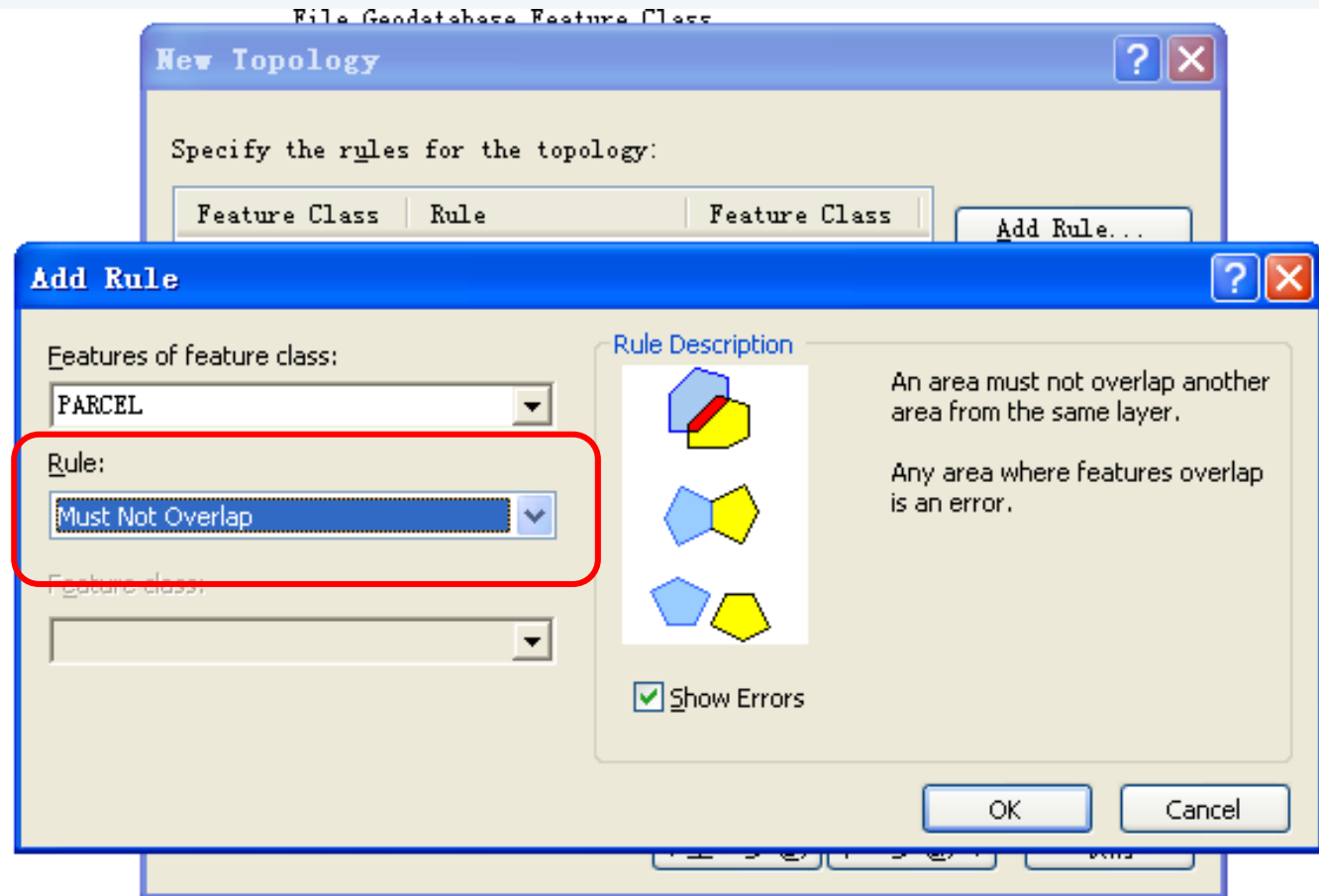
1 INTRODUCTION

2D CADASTRE SPACE VALIDATION

2D

A

ARCGIS



1 INTRODUCTION

3D CADASTRE SPACE VALIDATION

3D

```
graph LR; A[3D] --- B[A single 3D parcel validation technology]; A --- C[Ensure the validation (no overlap) among 3D parcels]; B --- Q[?]; C --- Q;
```

A single 3D parcel validation technology

Ensure the validation (no overlap) among 3D parcels

2 3D VALIDATION

3D CADASTRE SPACE VALIDATION

- **Verbree and Hang Si (2008) have employed Constrained Delaunay Tetrahedralization (CDT) to check the validity of a single 3D polyhedron.**
- **Brugman et al. (2011) developed a series of topological rules to validate a 3D topology structure for a 3D space partition.**
- **Thompson and Peter Van Oosterom (2011) extended these rules to axiomatic definitions to validate a 3D parcel and its relationship with adjoining parcels**

2 3D VALIDATION

3D CADASTRE SPACE VALIDATION

- **Karki et al. (2011) specifically discussed the data validation in 3D cadastre including a single 3D parcel and its relationships with other parcels.**

2 3D VALIDATION

3D CADASTRE SPACE VALIDATION

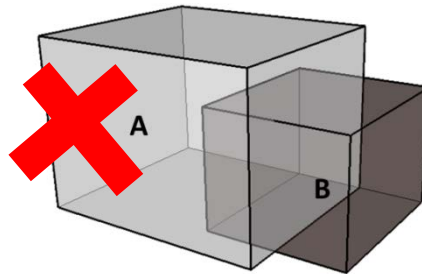
The four papers introduced or discussed the validation methods or rules mainly for single 3D parcel using computational geometry or topology rules.

But as to 3D topological relations identification, it needs more study to design practical algorithms or methods. And this paper will introduce a case for it.

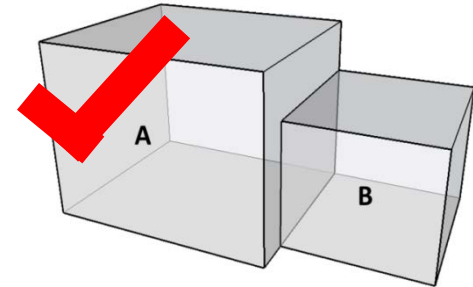
3 TOPOLOGICAL RELATIONS

Correct and incorrect topological relations

incorrect



correct



Topological
relations

Basic
Granularity

There is intersections
between A and B

There is no intersections
between A and B

Equal, Intersect
Cover, Contain

Touch, Disjoint

3 TOPOLOGICAL RELATIONS

incorrect topological relations

Basic Granularity



equal	cover	intersect	contain

3 TOPOLOGICAL RELATIONS

Correct topological relations in basic granularity

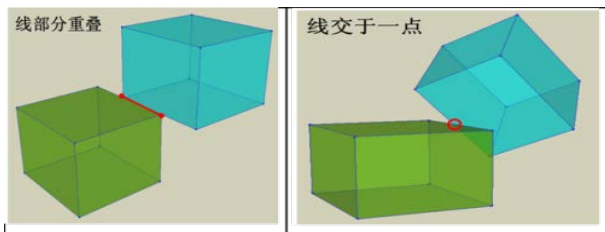
Touch relations in Dimension-Extended Model

Primitives	Detailed primitives	Equal	Intersect	Cover	Contain
Between n ID primitive and j D primitive ($i=j$)	Point and Point		None	None	None
	Edge and Edge				
	Face and Face				
Between n ID primitive and j D primitive ($i \neq j$)	Point and Edge	None	None	None	
	Point and Face	None	None	None	
	Edge and Face	None			

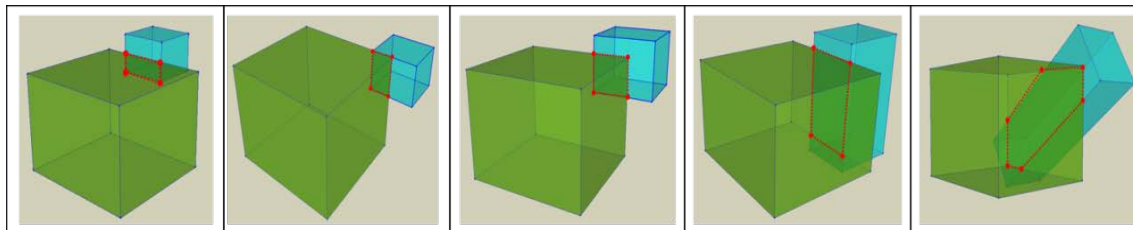
3 TOPOLOGICAL RELATIONS

correct topological relations — touch extension

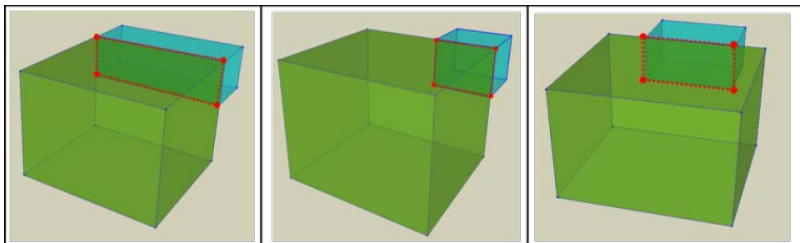
Edges Intersection



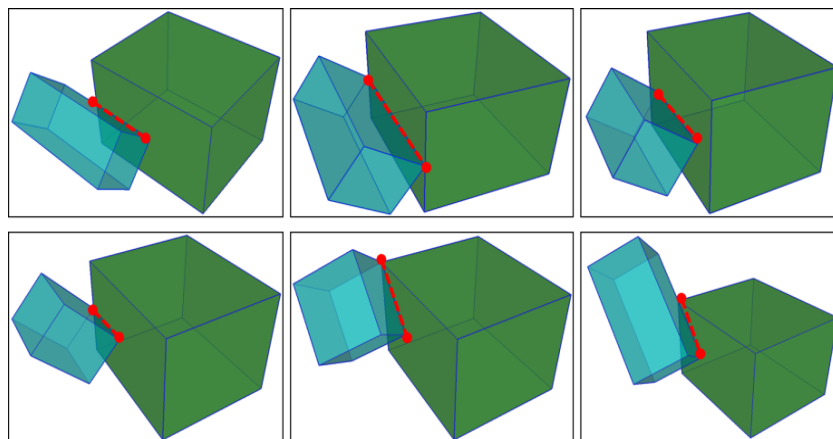
Faces intersection



Face covers face

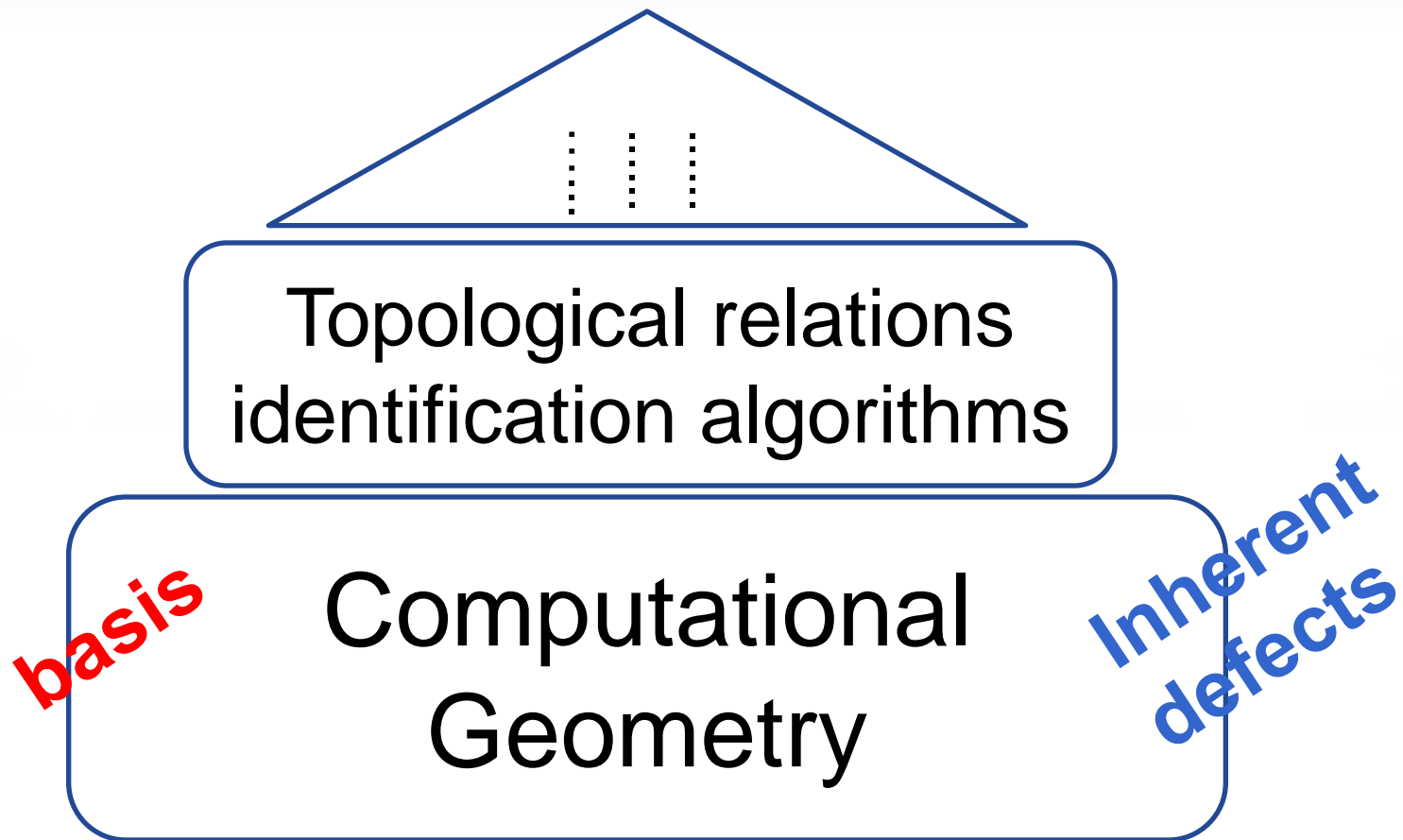


Face covers edge



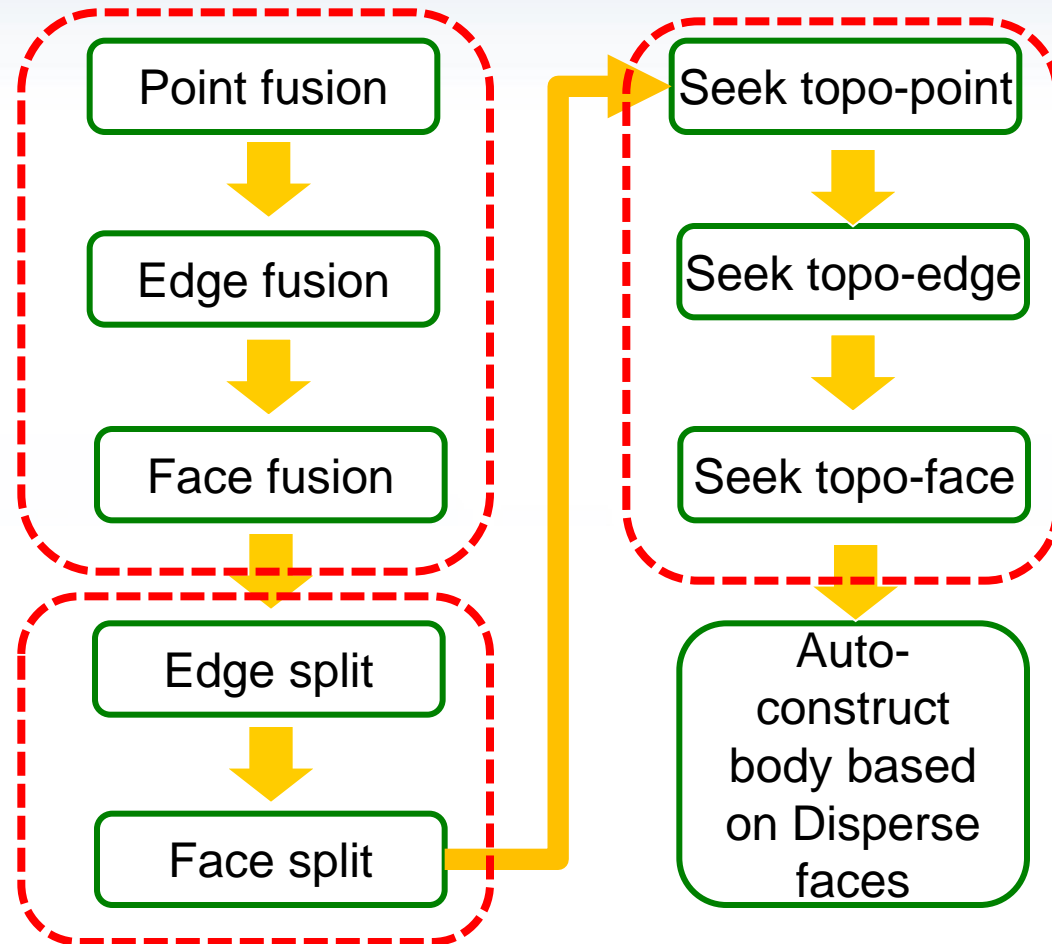
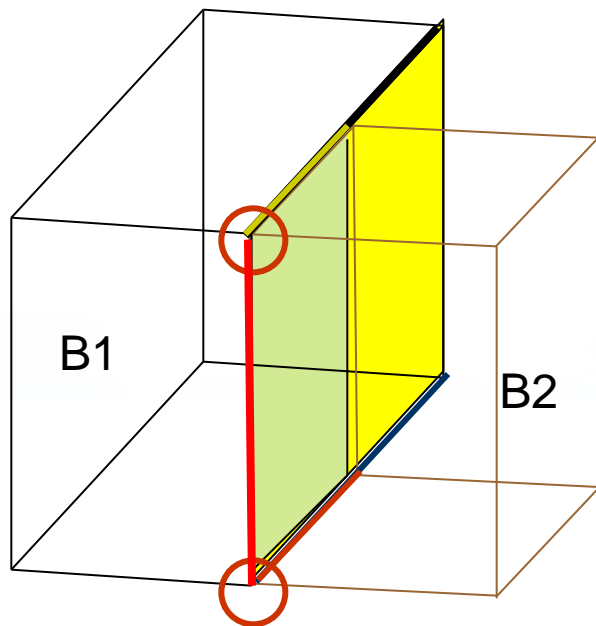
4 IDENTIFICATION OF TOPOLOGICAL RELATIONS

The basis of topological relations identification



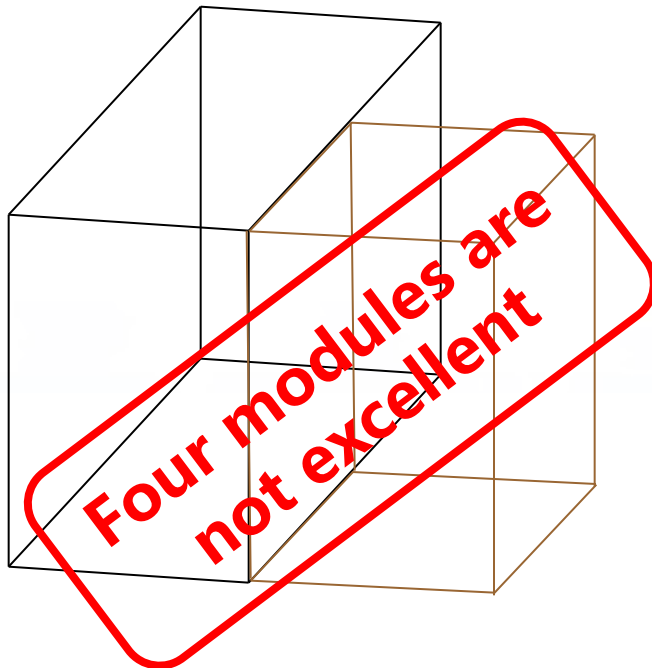
4 IDENTIFICATION OF TOPOLOGICAL RELATIONS

Automatically body-construct algorithm



4 IDENTIFICATION OF TOPOLOGICAL RELATIONS

Automatically body-construct algorithm



Redundant
primitives
unique

Seek topo-
primitives

public
part split

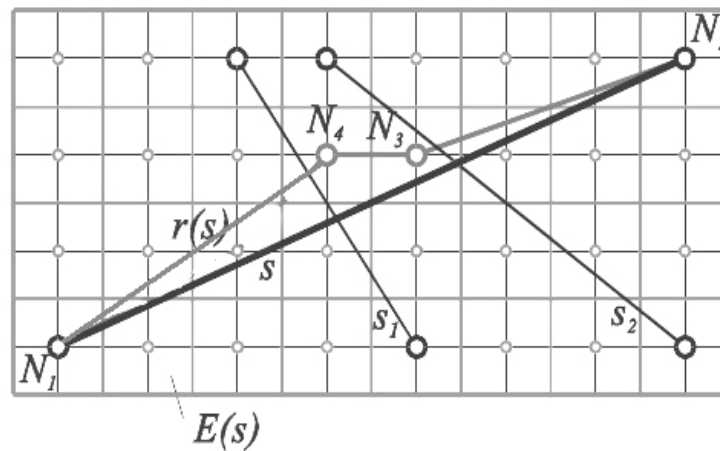
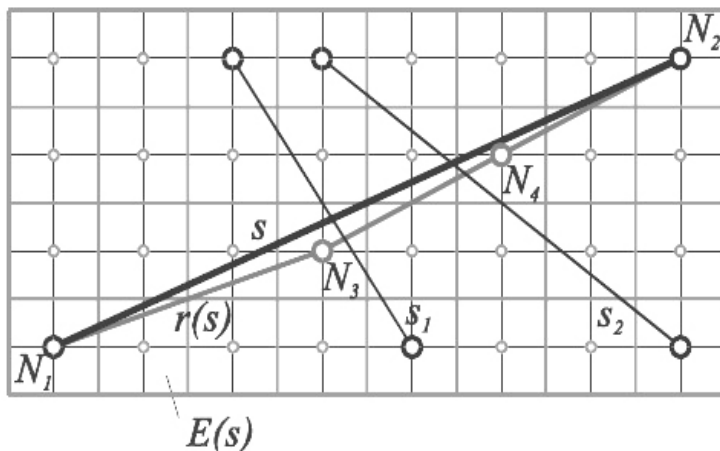
Auto-
construct
body
based on
Disperse
faces

4 IDENTIFICATION OF TOPOLOGICAL RELATIONS

Automatically body-construct algorithm

Split defect

Edge split : The results not unique



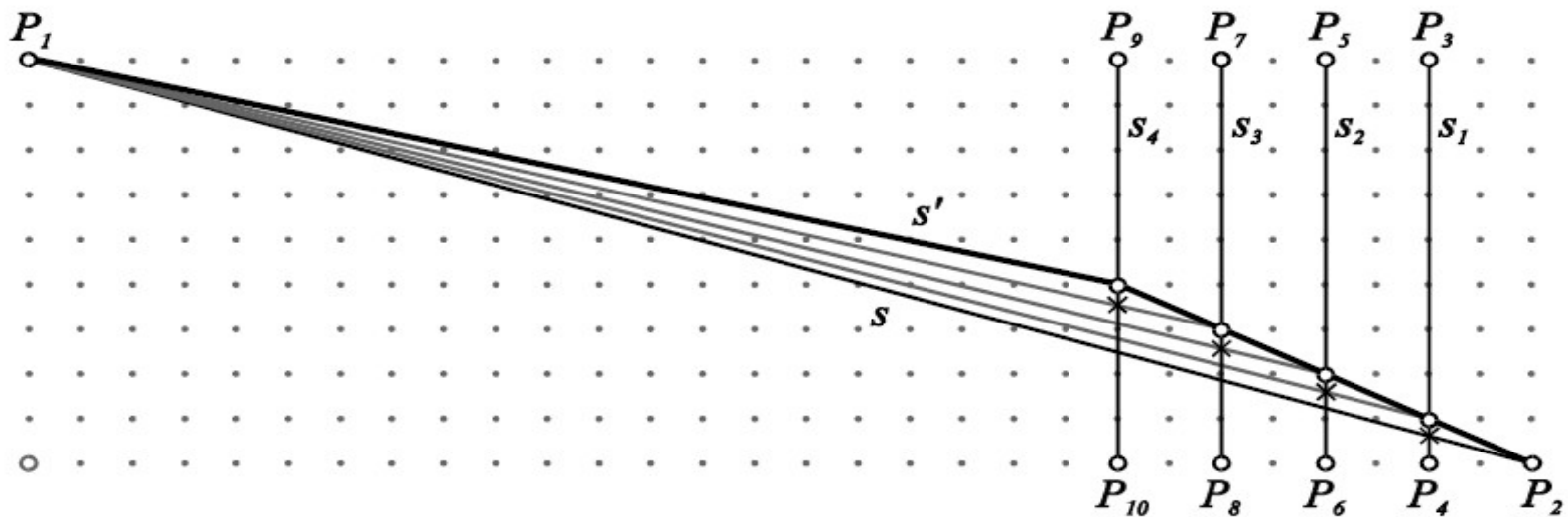
Werner Hölbling, Werner Kuhn, Andrew U. Frank. Finite-Resolution
Simplicial Complexes

4 IDENTIFICATION OF TOPOLOGICAL RELATIONS

Automatically body-construct algorithm

Split defect

Edge split : Cumulative offset



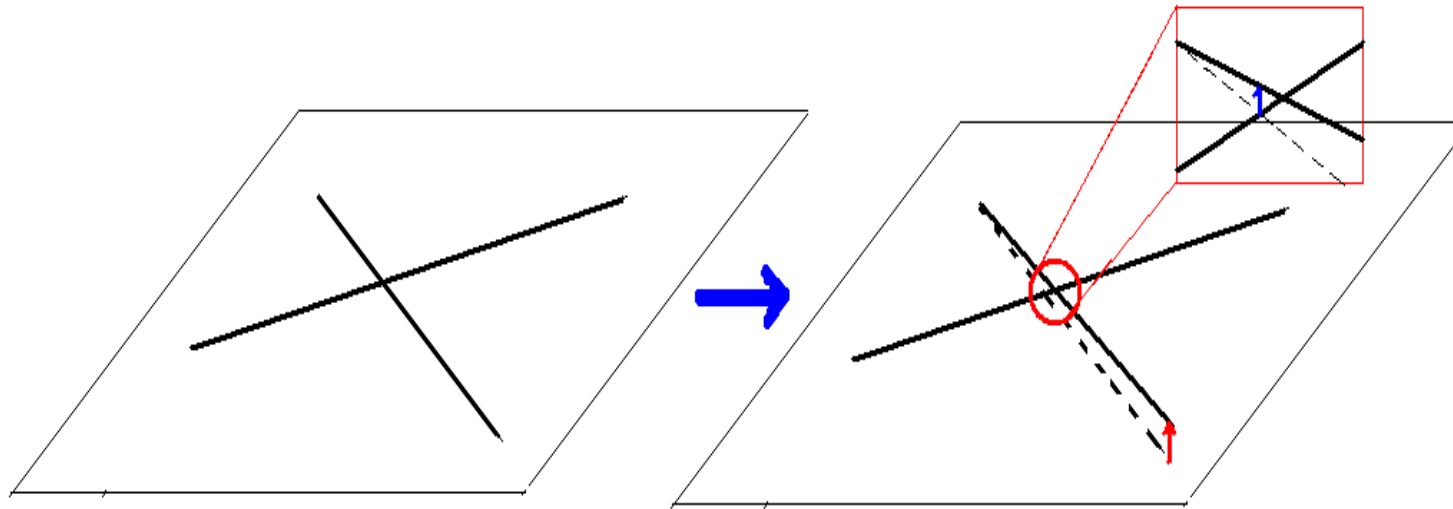
Werner Hölbling, Werner Kuhn, Andrew U. Frank. Finite-Resolution
Simplicial Complexes

4 IDENTIFICATION OF TOPOLOGICAL RELATIONS

Automatically body-construct algorithm

Split defect

Edge split : Data perturbation

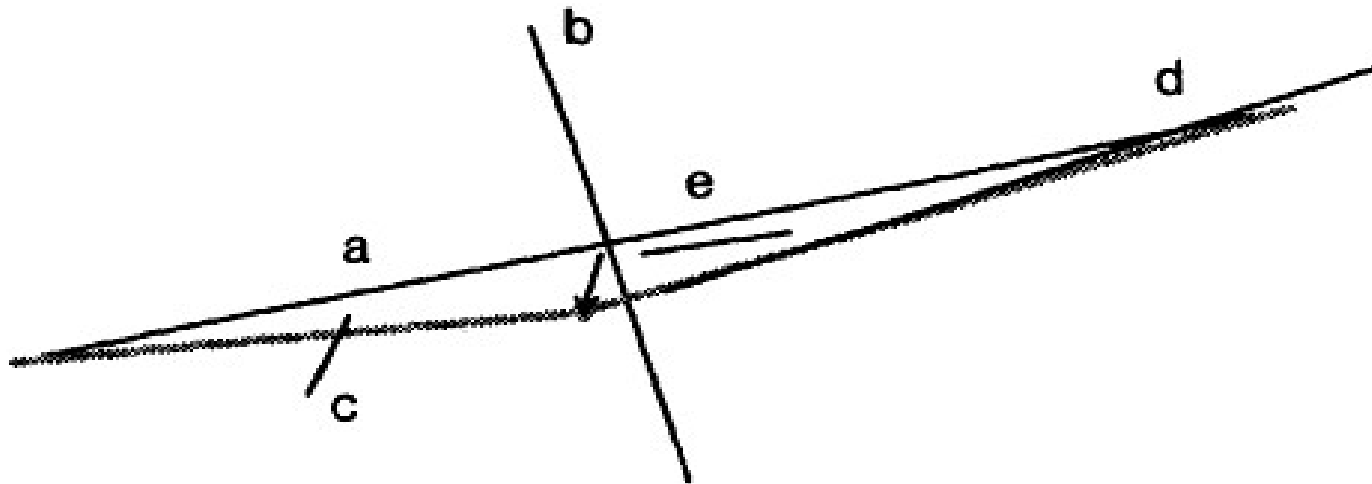


4 IDENTIFICATION OF TOPOLOGICAL RELATIONS

Automatically body-construct algorithm

Split defect

Edge split : Topology inconsistent



Daniel H. Greene, F. Frances Yao. FINITE-RESOLUTION
COMPUTATIONAL GEOMETRY

4 IDENTIFICATION OF TOPOLOGICAL RELATIONS

Automatically body-construct algorithm

Edge split error



Face split error

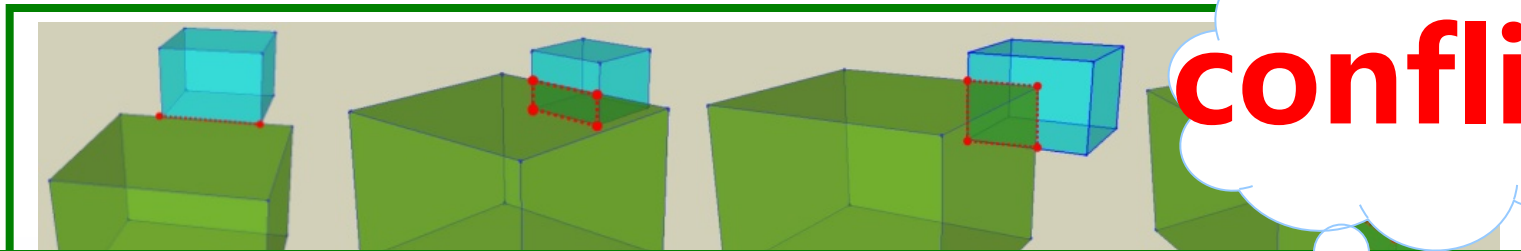
These defects will lead to
topology construction failed

4 IDENTIFICATION OF TOPOLOGICAL RELATIONS

Automatically body-construct algorithm

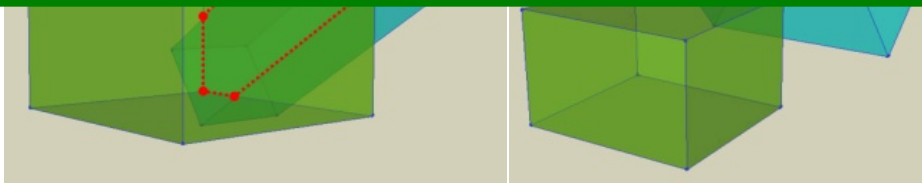
Split defect

Edge, face split : add new data



conflict

Cadastral map data with the force of law is
Unalterable (in china)



4 IDENTIFICATION OF TOPOLOGICAL RELATIONS

Automatically body-construct algorithm

These defects are inherent in the current 3D cadastral geometry algorithms, and can be avoided by using a method which will bring a series of updates to the current 3D cadastral data. This need **to seek a new 3D cadastral topology construction method**. This method can **cope with the various defects mentioned above**, simultaneously **ensure the legitimacy of the raw measurement data** of a 3D parcel.

Virtual element method

4 IDENTIFICATION OF TOPOLOGICAL RELATIONS

Virtual element method : Design Purpose

**Design
purpose**

1、 Don't break cadastre map data

2、 terminate the iterative error by split

3、 avoid Geometric element degeneration

4、 Different dimensional relations in touch

5、 topological check function

4 IDENTIFICATION OF TOPOLOGICAL RELATIONS

Virtual element method : Core Idea

Virtual element method

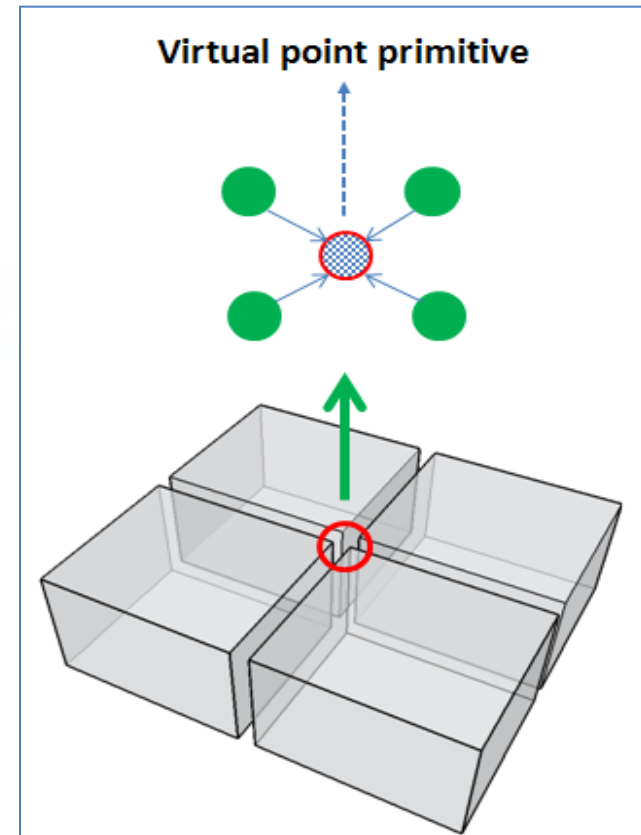
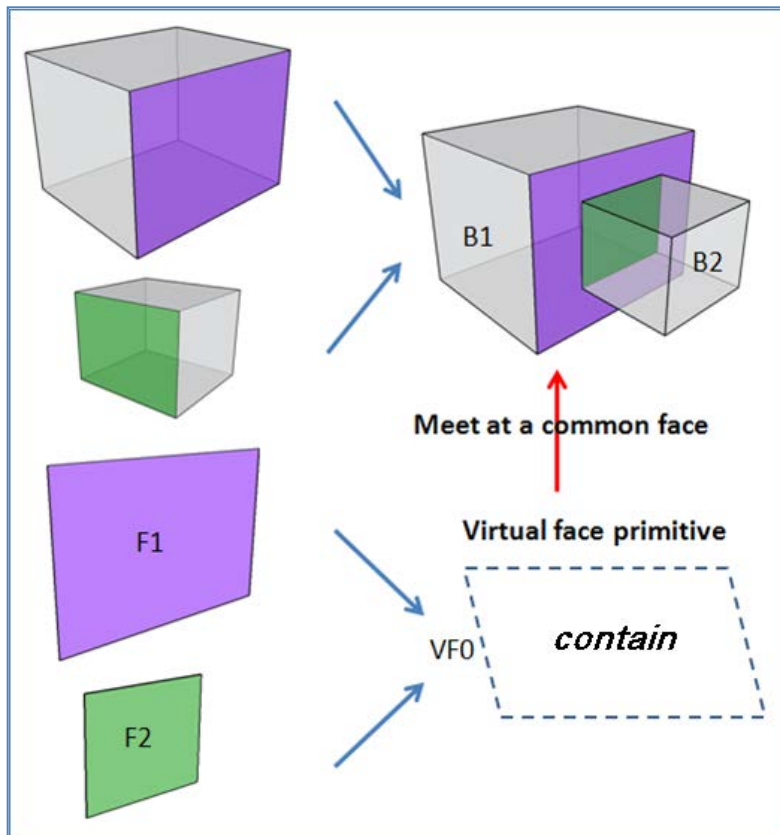
**core
idea**

- 1、 roles that represent relations among elements
- 2、 boundary combination reasoning method
- 3、 “compact / coupled” topological structure

4 IDENTIFICATION OF TOPOLOGICAL RELATIONS

Virtual element method : Core Idea

1、 role as virtual element

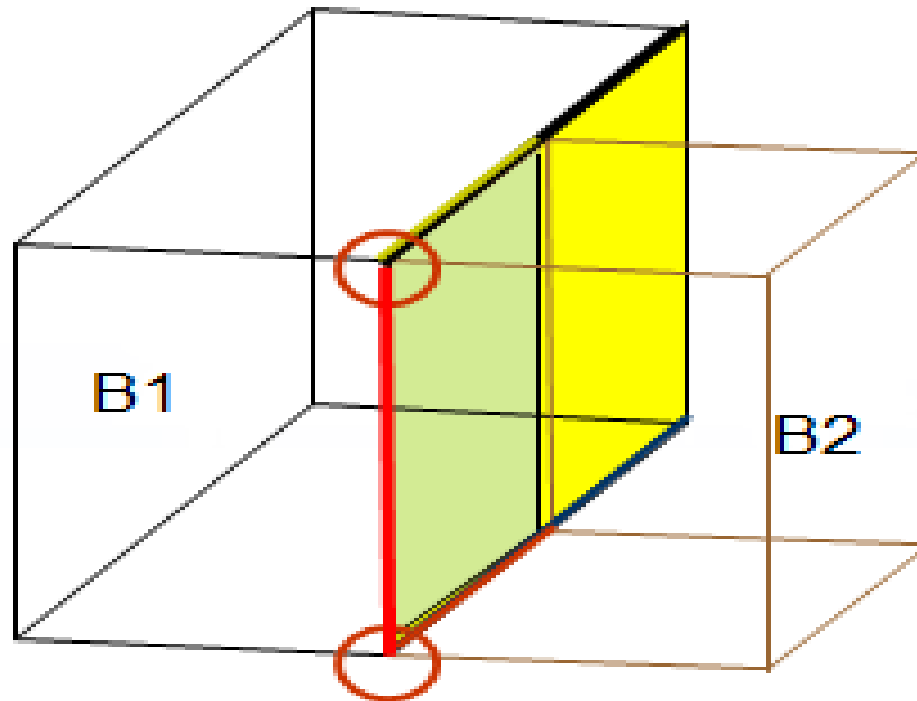
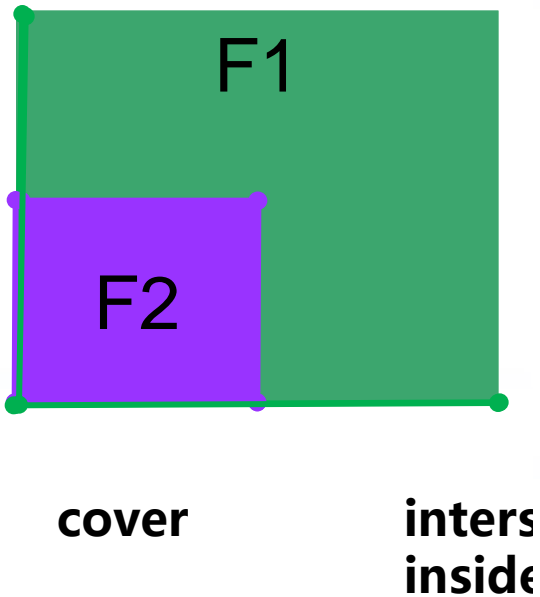


4 IDENTIFICATION OF TOPOLOGICAL RELATIONS

Virtual element method : Core Idea



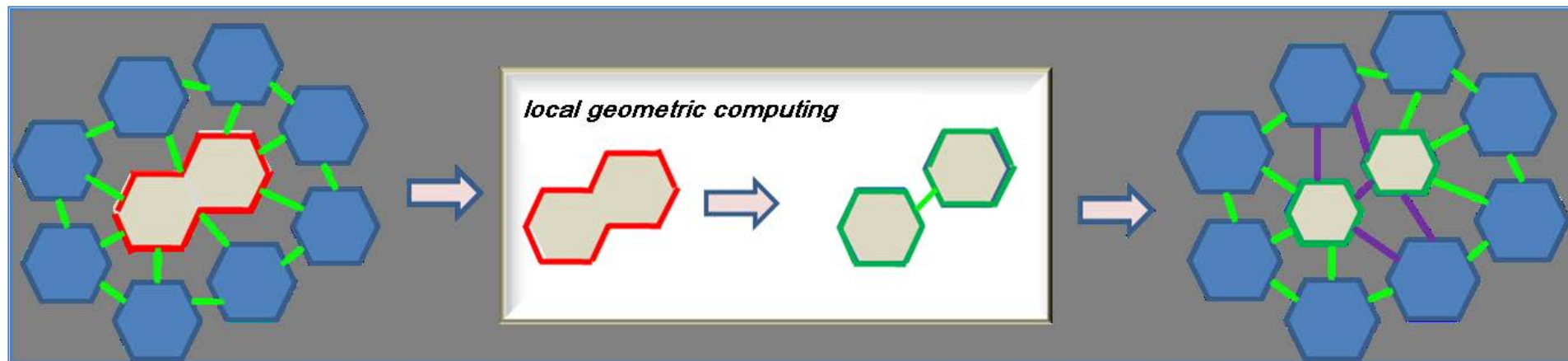
2、 boundary combination reasoning



4 IDENTIFICATION OF TOPOLOGICAL RELATIONS

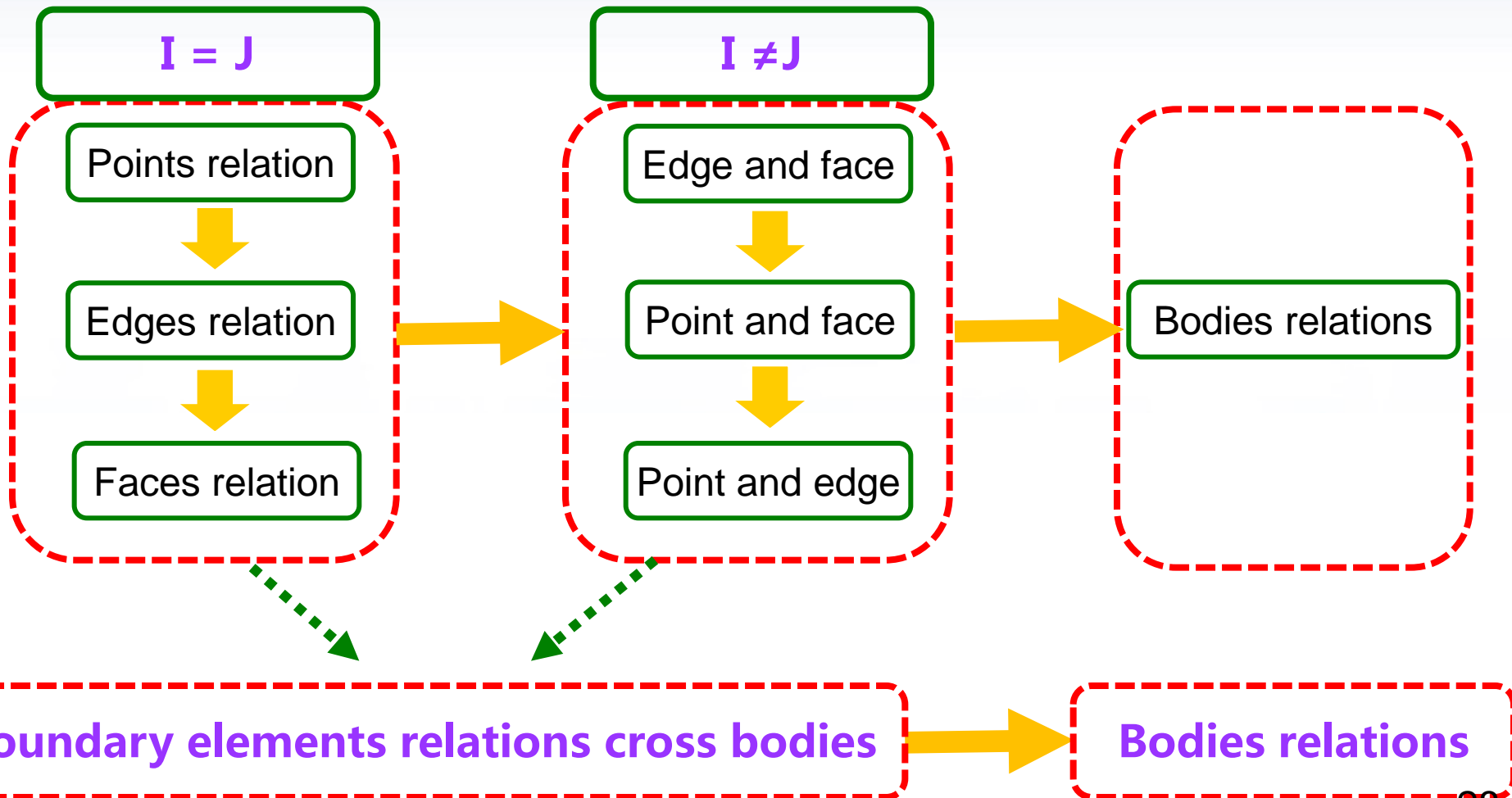
Virtual element method : Core Idea

3、 “compact / coupled” topological structure



4 IDENTIFICATION OF TOPOLOGICAL RELATIONS

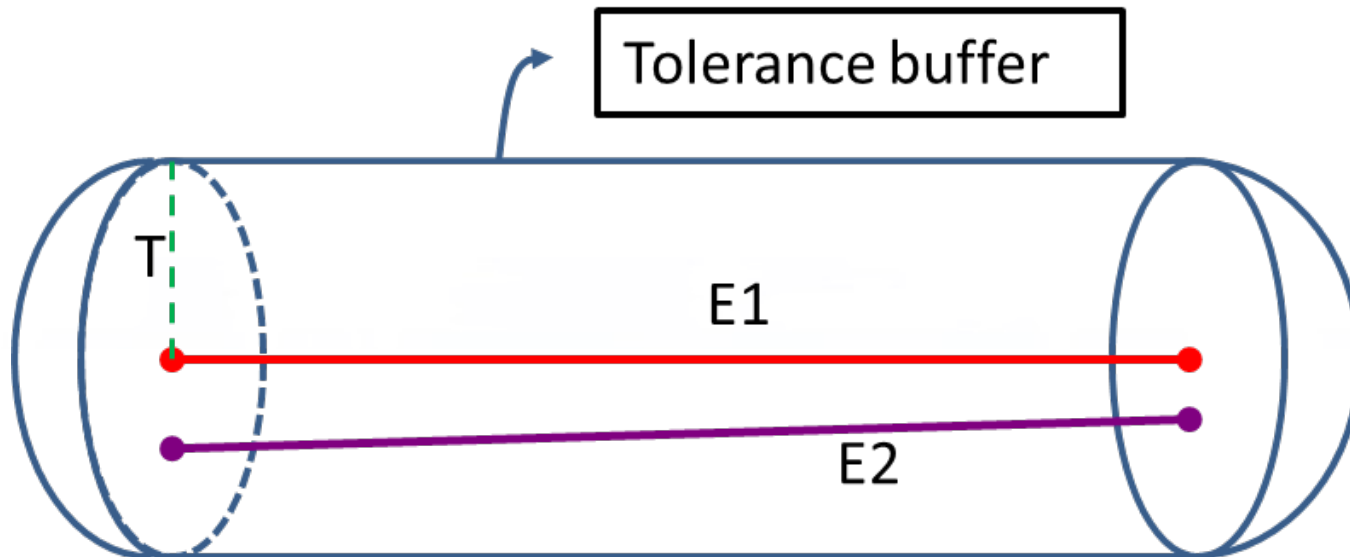
The algorithm design : general process



4 IDENTIFICATION OF TOPOLOGICAL RELATIONS

The algorithm design : several core Difficulties

1 edges relations reasoning in tolerance buffer

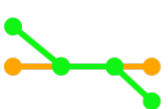
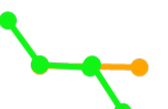
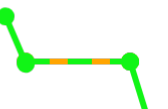


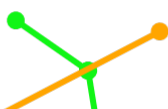
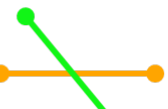
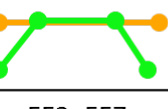




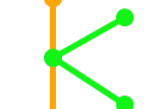


4 IDENTIFICATION OF TOPOLOGICAL RELATIONS

The algorithm design : several core Difficulties

2 faces relations

Boundary
combinational
reasoning
method

两个环交 叠于一维 交叠	交叠1	交叠2	交叠3	交叠4
				
	EE3 EE7	EE2 EE4 EE7	EE1 EE4	EE5 EE7
两个环交 错于零维 交错	交错1	交错2	交错3	
				
	EE4	EE7	EE6	
两个环重 叠于一维 重叠	重叠1	重叠2	重叠3	重叠4
				
	EE3 EE7	EE2 EE4 EE7	EE1 EE4	EE5 EE7
两个环相 切于零维 相切	相切1	相切2		
				
	EE4	EE7		

Local relations
among arcs



Local relations
combination



Faces relations
By reasoning

4 IDENTIFICATION OF TOPOLOGICAL RELATIONS

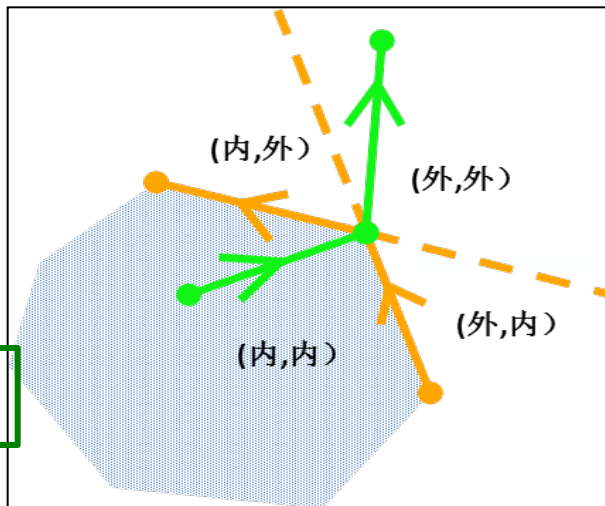
The algorithm design : several core Difficulties

2 faces relations reasoning operator

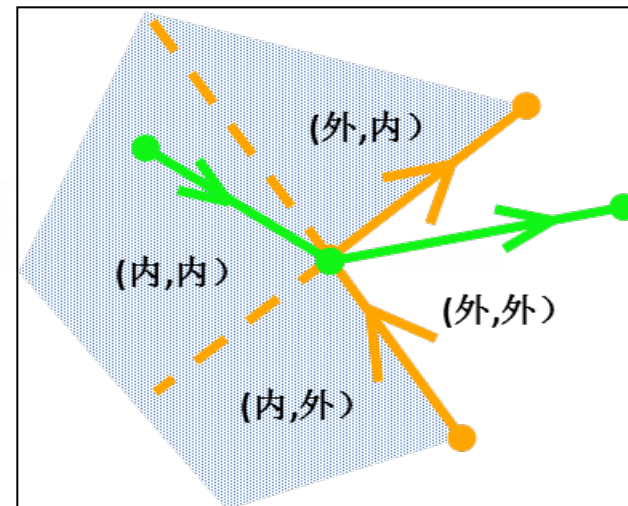
Local relations Identification

2D space

Operator 1



Vector distinguish method



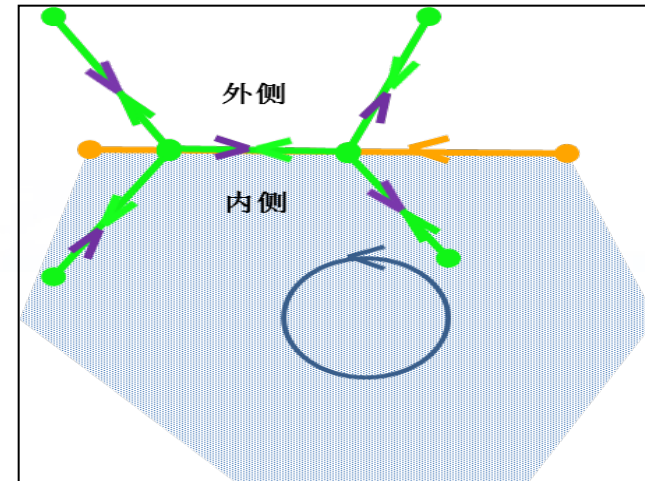
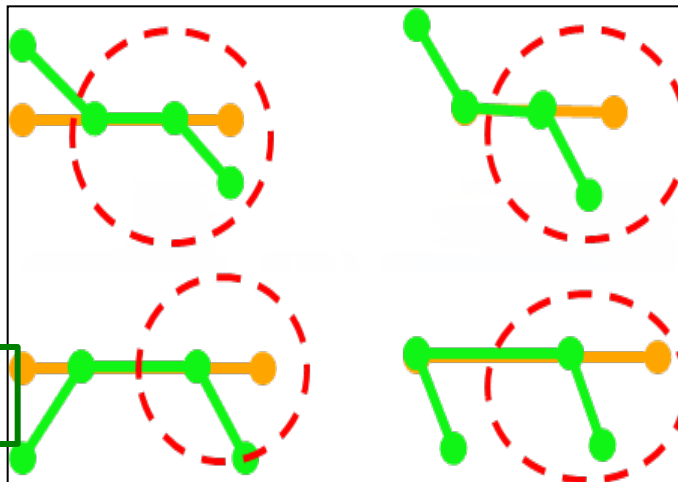
A collection of four-tuple : $S = \{ (\text{Protruding / Concave}), (\text{start/end}), (1/2), (1/2) \}$. The elements is unique and mutually exclusive

4 IDENTIFICATION OF TOPOLOGICAL RELATIONS

The algorithm design : several core Difficulties

2 faces relations reasoning operator

operator2

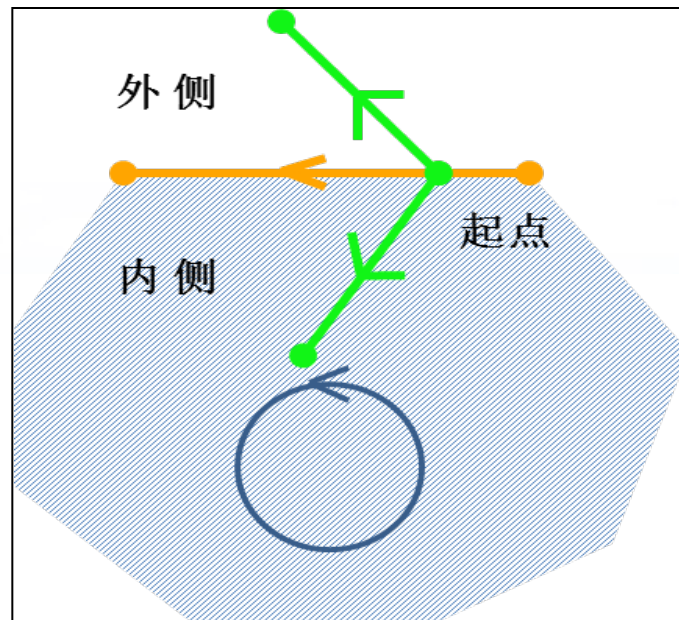
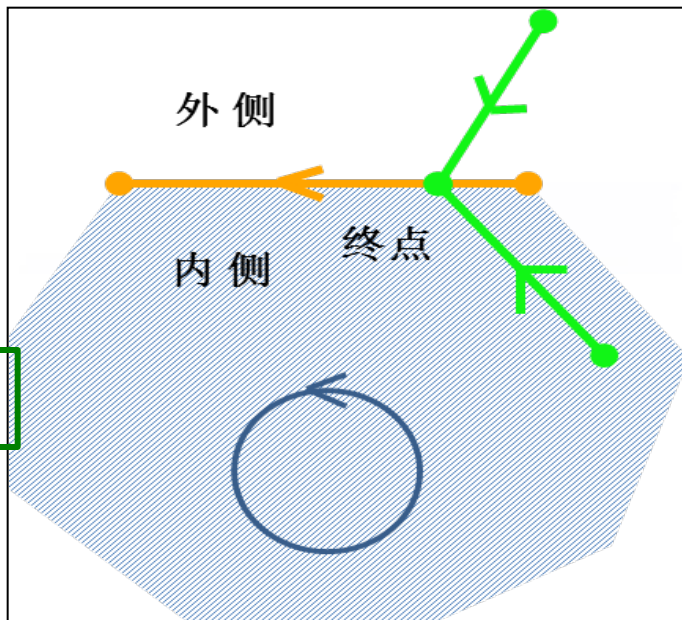


4 IDENTIFICATION OF TOPOLOGICAL RELATIONS

The algorithm design : several core Difficulties

2 faces relations reasoning operator

operator3



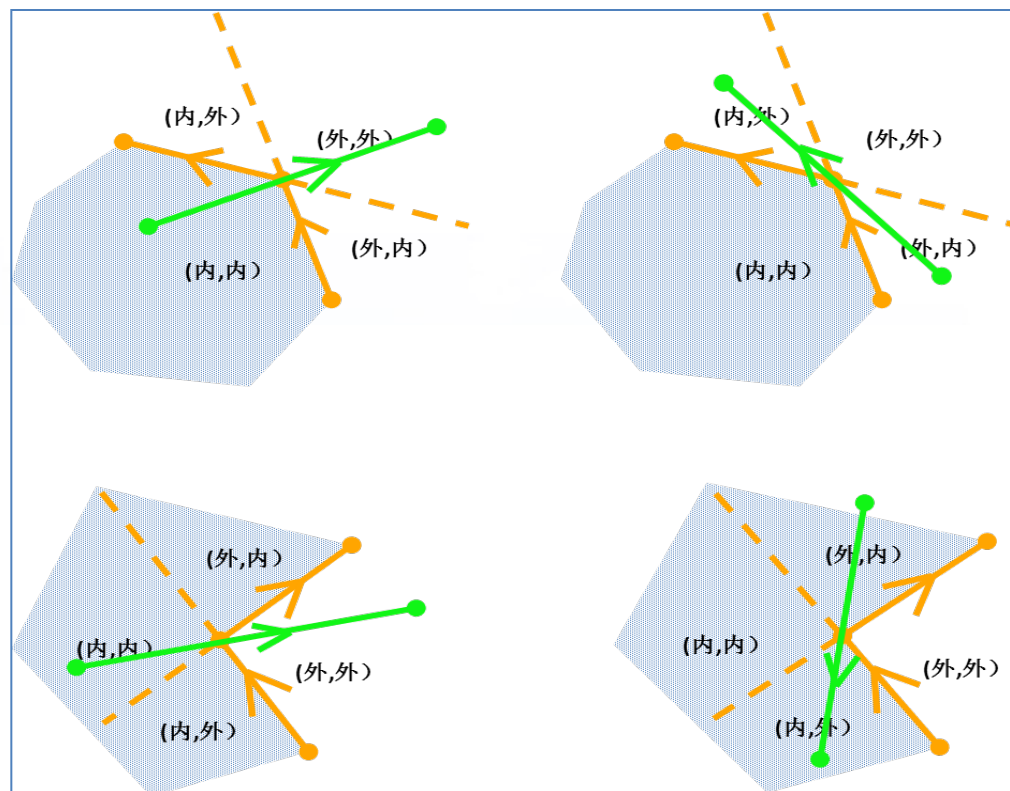
2D space

4 IDENTIFICATION OF TOPOLOGICAL RELATIONS

The algorithm design : several core Difficulties

2 faces relations reasoning operator

operator4



2D space

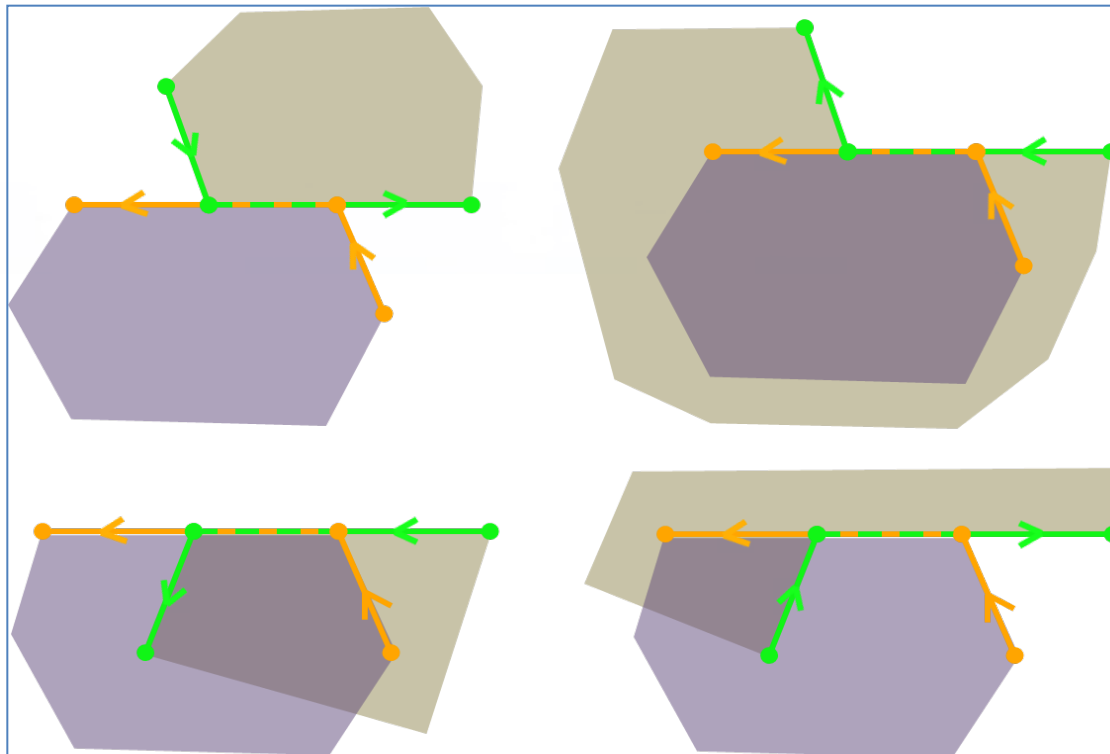
4 IDENTIFICATION OF TOPOLOGICAL RELATIONS

The algorithm design : several core Difficulties

2 faces relations reasoning operator

operator5

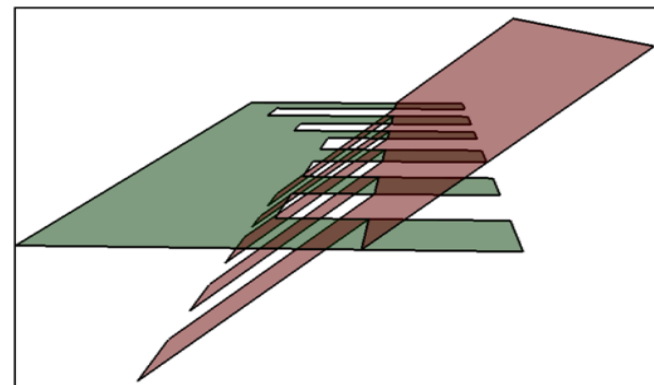
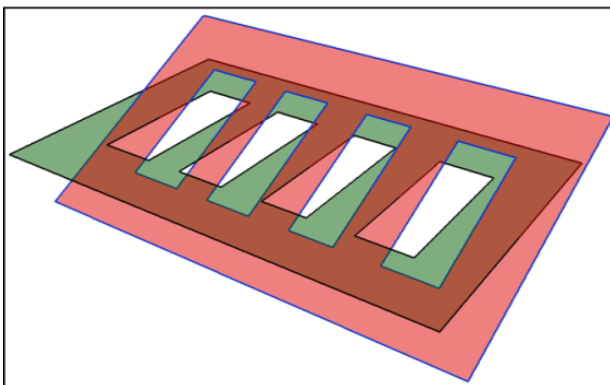
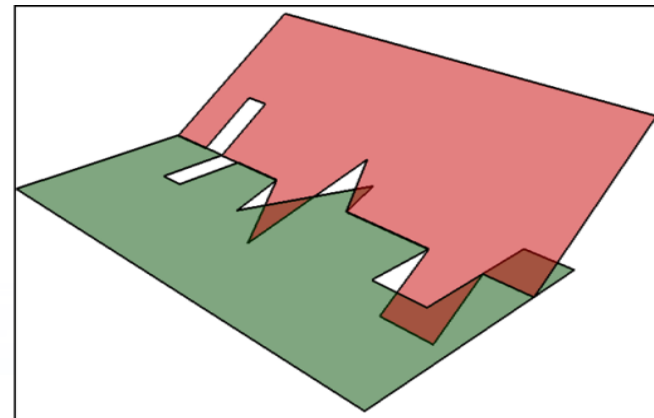
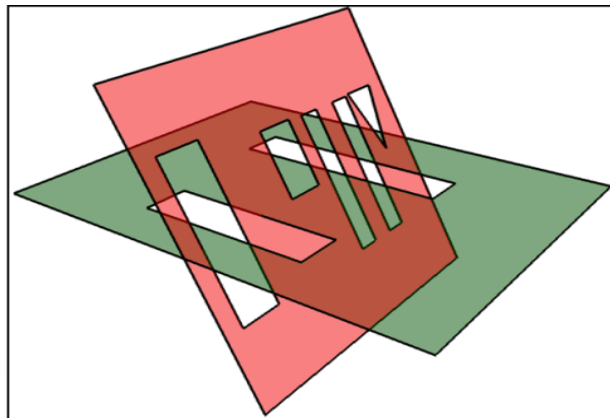
2D space



4 IDENTIFICATION OF TOPOLOGICAL RELATIONS

The algorithm design : several core Difficulties

2 faces relations reasoning - pure computational geometry

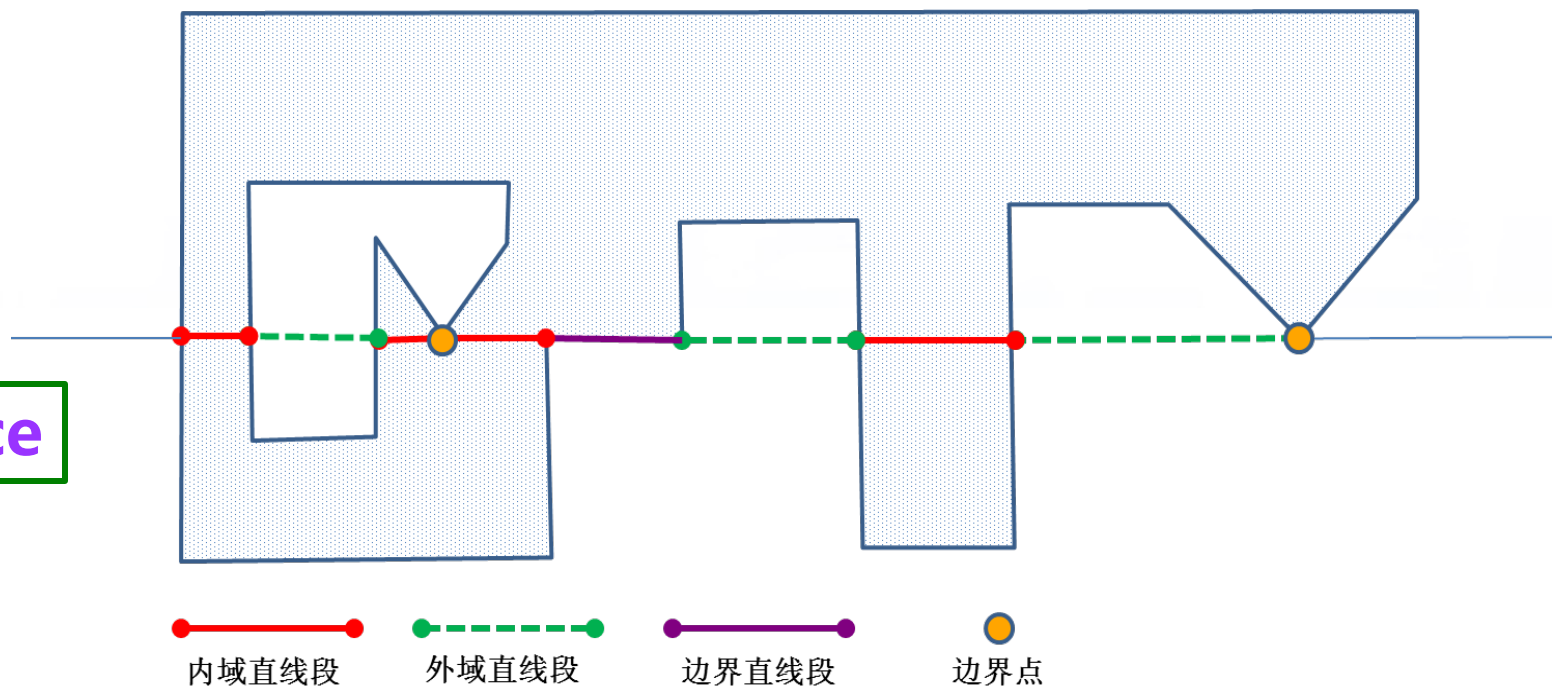


3D space

4 IDENTIFICATION OF TOPOLOGICAL RELATIONS

The algorithm design : several core Difficulties



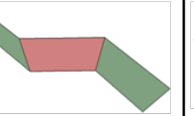



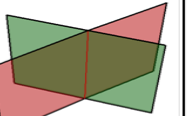







2 faces relations reasoning - pure geometric computing



4 IDENTIFICATION OF TOPOLOGICAL RELATIONS

The algorithm design : several core Difficulties

4 bodies relations

两个表面 交叠于二维	交叠1	交叠2	交叠3	交叠4
				
交叠	FF5 FF6	FF2 FF3 FF6	FF1 FF3	FF4 FF6
两个表面 交错于一维	交错1	交错2	交错3	
				
交错	FF3	FF6	FF7	
两个表面 重叠于二维	重叠1	重叠2	重叠3	重叠4
				
重叠	FF5 FF6	FF2 FF3 FF6	FF1 FF3	FF4 FF6
两个表面 相切于一维和零维	相切1	相切2	相切3	
				
相切	FF3	FF6		

Identify Surface local relations



Local relations combination

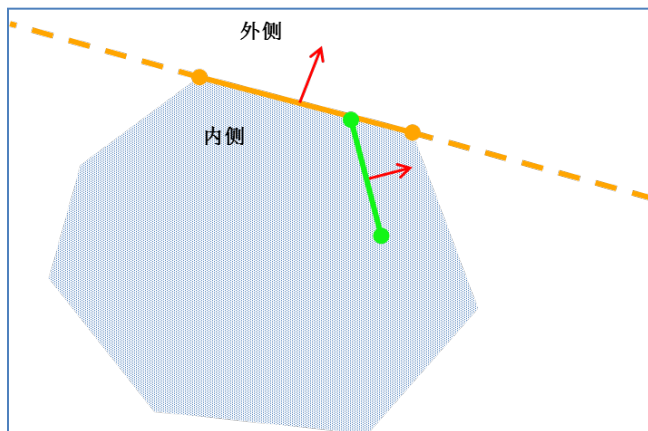
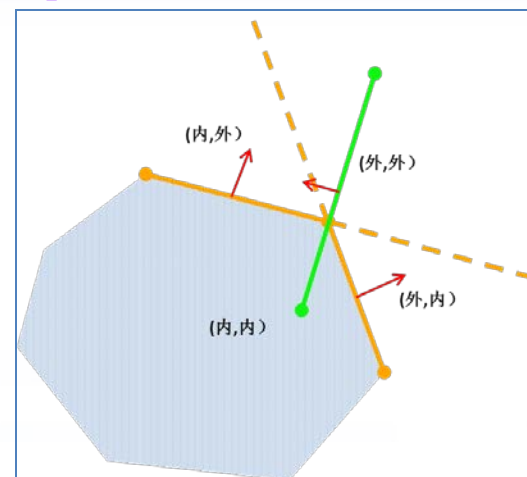
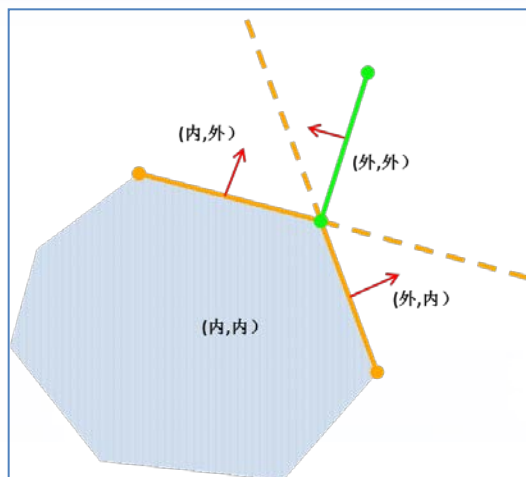


Bodies relation reasoning

4 IDENTIFICATION OF TOPOLOGICAL RELATIONS

The algorithm design : several core Difficulties

4 bodies relations reasoning operator

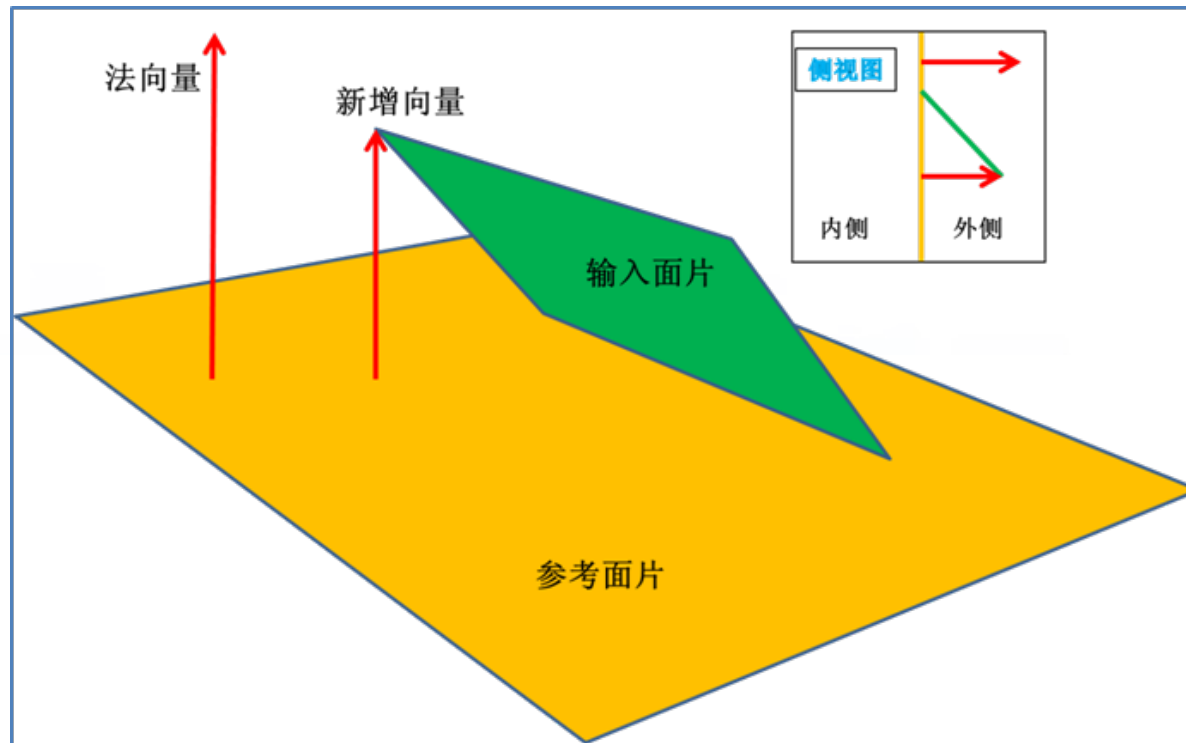


three operators

4 IDENTIFICATION OF TOPOLOGICAL RELATIONS

The algorithm design : several core Difficulties

3 bodies relation—vector angle judgment method



3 CONCLUSION

The algorithm in this paper can identify correct and incorrect topological relations among bodies. Therefore it could be used as topology checking module of a 3D cadastre management system. The algorithm has two main design purposes:

- 1) resolving the 3-dimensional parcel conflict and guarantee its unique and exclusive legitimate space;
- 2) correct topological relations represented in the underlying topological data structure and stored in a database could be the basis for the following spatial analysis.



THAT'S ALL! THANKS